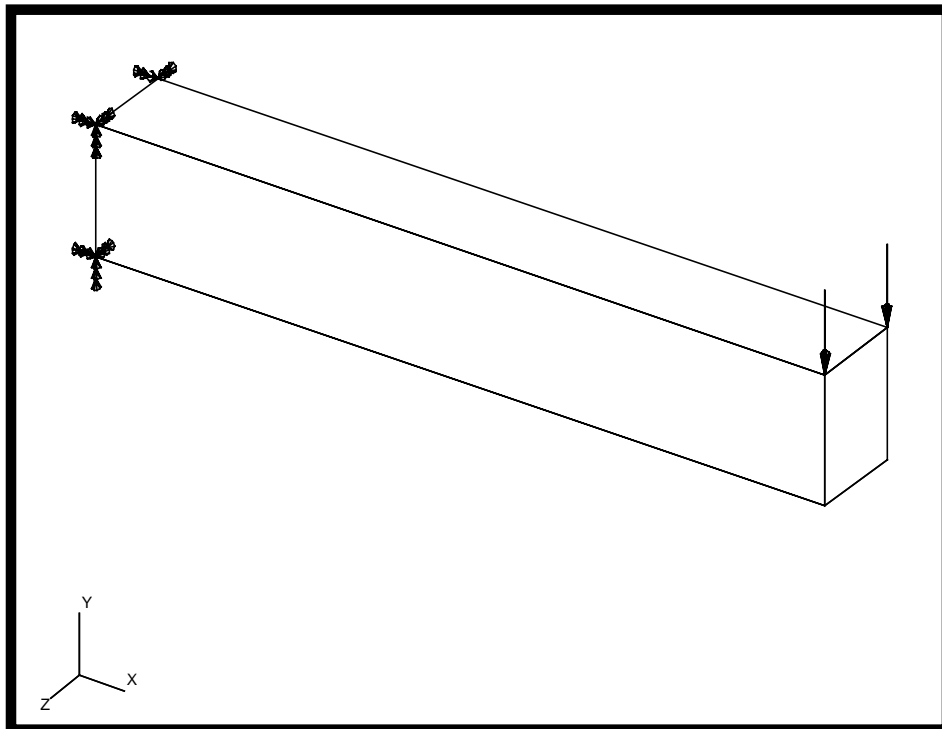


---

## APPENDIX D

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### *CBAR Element Shear Factor, $K$*



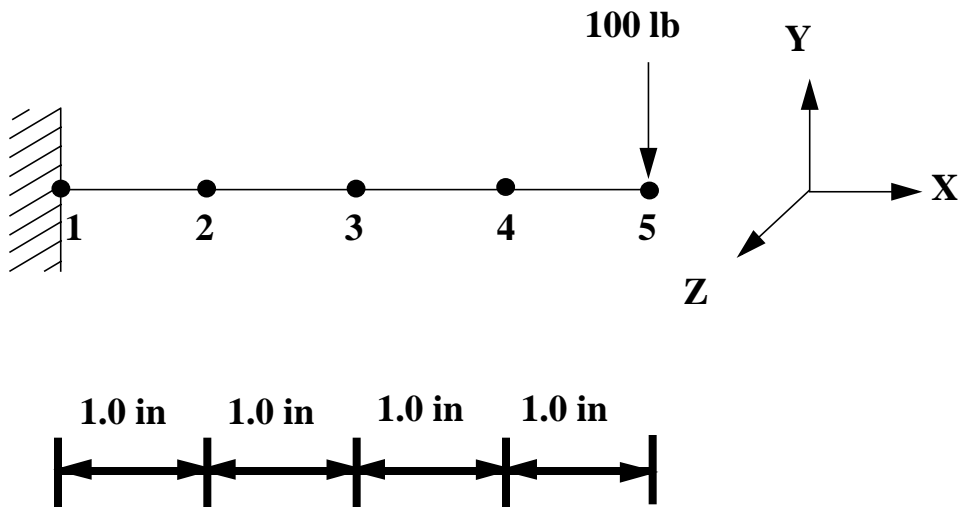
#### **Objectives:**

- Model a loaded cantilever beam with CBAR elements, including shear factors in element properties.
- Create a revised model which does not include shear factors.
- Compare both results with theory.



**Model Description:**

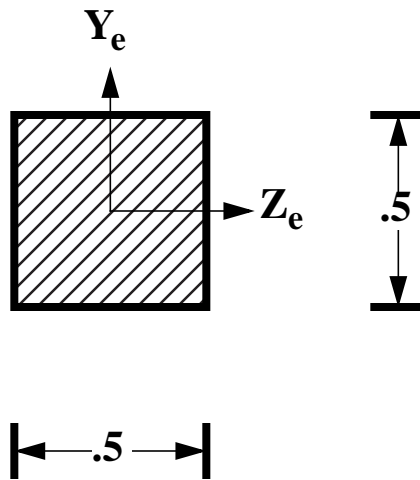
Illustrate the effect of the shear factor, K, on a cantilevered beam under a transverse load.



Material = aluminum  
E = 10.06E6 psi  
v = 0.3

---

Modeling the CBAR elements with an orientation vector of 0., 1., 0. results in the cross section:



$$\begin{aligned} A &= 0.25 \text{ in}^2 \\ I_1 &= I_2 = 0.0052 \text{ in}^4 \\ J &= 0.0088 \text{ in}^4 \end{aligned}$$

Since the cross-section is square,  $K = 5/6 = 0.8333$ .

## Suggested Exercise Steps:

- Open a new database.
- Create a curve and mesh it with bar elements (CBAR). Use the meshing feature so that elements and nodes (GRID) will be generated automatically by MSC/PATRAN.
- Define material (MAT1) and element properties (PBAR). Be certain to include shear factors in element property definitions.
- Apply a fixed boundary condition (SPC1) at one end of the beam and a transverse force to the free end of the beam (FORCE).
- Use the load and boundary sets to define a loadcase.
- Prepare the model for a Linear Static analysis (SOL 101 & PARAMs).
- Generate and submit input file to the MSC/NASTRAN solver.
- Create a revised MSC/NASTRAN input file without referencing shear factors in element property definitions.
- Compare both results with theory.

---

## Results:

The shear factors  $K_y$  and  $K_z$  define the shear displacements  $V_{ys}$  and  $V_{zs}$  in the element coordinate system. The total displacement of the reference axis is

$$V_y = V_{yb} + V_{ys}$$

where  $V_{yb}$  = displacement due to bending.

From hand calculations, the predicted maximum displacement due to bending is:

$$\frac{PL^3}{3EI} = \frac{100(4)^3}{3(10.E6)(0.0052)} = 0.04102564 \text{ in}$$

The maximum displacement due to shear is:

$$\frac{\sqrt{L}}{AG} = \frac{100(4)}{0.833(0.25)(3.846E6)} = 0.000499 \text{ i}$$

Total displacement =  $0.04102564 + 0.000499 = 0.041525 \text{ in}$

The following represent first, the beam modeled with shear factors, and second, the beam modeled without shear factors.

	Tip Deflection
Model w/ shear factors	-0.04153
Model w/o shear factors	-0.04103
Theory	-0.04153

**Sample NASTRAN Input File:**

```

ID SEMINAR, Appendix D
SOL 101
TIME 60
CEND
SEALL = ALL
SUPER = ALL
TITLE = CBAR Element Shear Factor, K
ECHO = SORT
MAXLINES = 999999999
SUBCASE 1
SUBTITLE=Default
  SPC = 2
  LOAD = 2
  DISPLACEMENT(SORT1,REAL)=ALL
  SPCFORCES(SORT1,REAL)=ALL
  STRESS(SORT1,REAL,VONMISES,BILIN)=ALL
BEGIN BULK
PARAM  POST  -1
PARAM  PATVER 3.
PARAM  AUTOSPC YES
PARAM  INREL  0
PARAM  ALTRED NO
PARAM  COUPMASS 0
PARAM  K6ROT  0.
PARAM  WTMASS .00259
PARAM  GRDPNT 0
PARAM,NOCOMPS,-1
PBAR  1  1  .25  .0052  .0052  .0088  + A
+  A .25  .25  .25  -.25  -.25  .25  -.25  -.25  + B
+  B .8333  .8333
CBAR  1  1  1  2  0.  1.  0.
CBAR  2  1  2  3  0.  1.  0.

```

---

```
CBAR 3 1 3 4 0. 1. 0.
CBAR 4 1 4 5 0. 1. 0.
MAT1 1 1.+7 .3
GRID 1 0. 0. 0.
GRID 2 1. 0. 0.
GRID 3 2. 0. 0.
GRID 4 3. 0. 0.
GRID 5 4. 0. 0.
SPCADD 2 1
LOAD 2 1. 1. 1
SPC1 1 123456 1
FORCE 1 5 0 100. 0. -1. 0.
ENDDATA
```